





T. HOEFLER

## **High-Performance Communication in Machine Learning**

Keynote at the 13th International Conference on Parallel Processing and Applied Mathematics



#### https://www.arxiv.org/abs/1802.09941

Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis

TAL BEN-NUN\* and TORSTEN HOEFLER, ETH Zurich

Deep Neural Networks (DNNs) are becoming an important tool in modern computing applications. Accelerating their training is a major challenge and techniques range from distributed algorithms to low-level circuit design. In this survey, we describe the problem from a theoretical perspective, followed by approaches for its parallelization. Specifically, we present trends in DNN architectures and the resulting implications on parallelization strategies. We discuss the different types of concurrency in DNNs; synchronous and asynchronous stochastic gradient descent; distributed system architectures; communication schemes; and performance modeling. Based on these approaches, we extrapolate potential directions for parallelism in deep learning.

CCS Concepts: • General and reference → Surveys and overviews; • Computing methodologies → Neural networks; Distributed computing methodologies; Parallel computing methodologies; Machine learning;

Additional Key Words and Phrases: Deep Learning, Distributed Computing, Parallel Algorithms

#### ACM Reference format:

Tal Ben-Nun and Torsten Hoefler 2018. Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis 60 pages.

#### 1 INTRODUCTION

Machine Learning, and in particular Deep Learning [LeCun et al. 2015], is a field that is rapidly taking over a variety of aspects in our daily lives. In the core of deep learning lies the Deep Neural Network (DNN), a construct inspired by the interconnected nature of the human brain. Trained properly, the expressiveness of DNNs provides accurate solutions for problems previously thought to be unsolvable, simply by observing large amounts of data. Deep learning has been successfully implemented for a plethora of subjects, ranging from image classification [Huang et al. 2017], through speech recognition [Amodei et al. 2016] and medical diagnosis [Cireşan et al. 2013], to autonomous driving [Bojarski et al. 2016] and defeating human players in complex games [Silver et al. 2017] (see Fig. 1 for more examples).







## What is Deep Learning good for?



Digit Recognition

Object Classification
Segmentation
Image Captioning

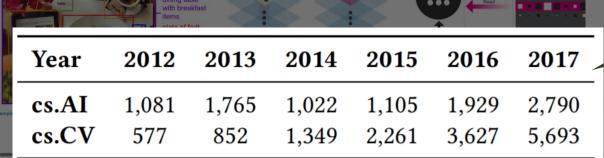
Gameplay Al Translation

**Neural Computers** 

Gigantic Language Models

Towards Real Physics

## A very active area of research!



23 papers per day!

that
that
are
pink
white
and
white
and

number of papers per year

1989

2012 2013 2014

2016

2017

2018

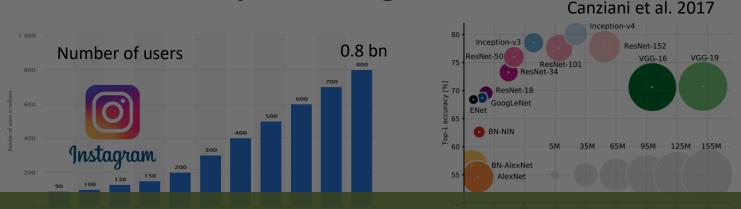
2019

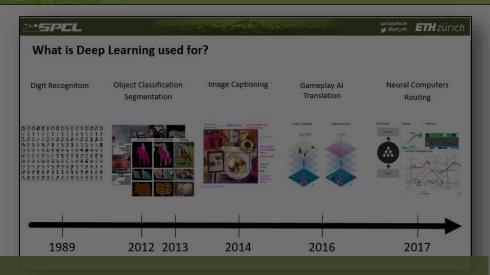






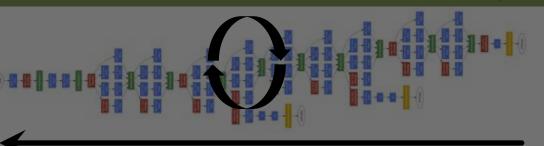
## **How does Deep Learning work?**





## Deep Learning is Supercomputing!







layer-wise weight update

- ImageNet (1k): 180 GB
- ImageNet (22k): A few TB
- Industry: Much larger

- 100-200 layers deep
- ~100M-2B parameters
- 0.1-8 GiB parameter storage

- 10-22k labels
- growing (e.g., face recognition)
- weeks to train

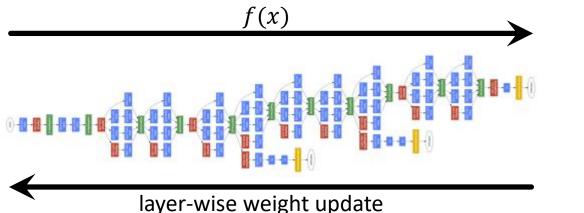


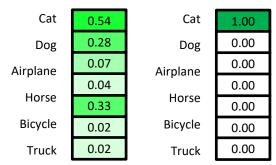




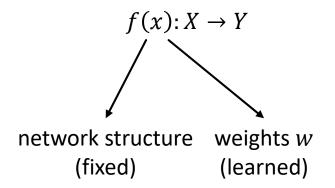
## A brief theory of supervised deep learning



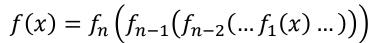


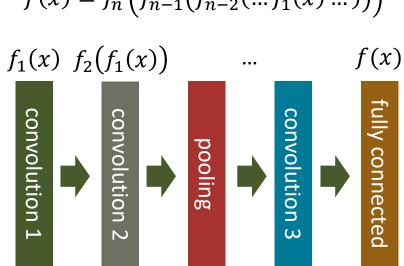


labeled samples  $x \in X \subset \mathcal{D}$ 



 $w^* = \operatorname{argmin}_{w \in \mathbb{R}^d} \mathbb{E}_{x \sim \mathcal{D}}[\ell(w, x)]$ 





label domain Y

true label l(x)

$$\ell_{sq}(w,x) = (f(x) - l(x))^2$$

$$\ell_{0-1}(w, x) = \begin{cases} 0 & f(x) = l(x) \\ 1 & f(x) \neq l(x) \end{cases}$$

$$\ell_{ce}(w,x) = -\sum_{i} l(x)_{i} \cdot \log \frac{e^{f(x)_{i}}}{\sum_{k} e^{f(x)_{k}}}$$







## **Stochastic Gradient Descent**

1:
2:
3:
4:
5:
6:
7:
8:
9:
10:
11:

 $w^* = \operatorname{argmin}_{w \in \mathbb{R}^d} \mathbb{E}_{x \sim \mathcal{D}}[\ell(w, x)]$ 

 $f_1(x)$ 

convolution 1

 $f_2(f_1(x))$ 

convolution 2

pooling

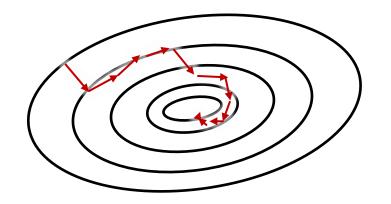
...

convolution 3

f(x)

fully connected

• Layer storage =  $|w_l| + |f_l(o_{l-1})| + |\nabla w_l| + |\nabla o_l|$ 



Learning Rate  $w^{(t+1)} = w^{(t)} - \eta \cdot \nabla \ell(w^{(t)}, z) = w^{(t)} - \eta \cdot \nabla w^{(t)}$  Adaptive Learning Rate  $w^{(t+1)} = w^{(t)} - \eta_t \cdot \nabla w^{(t)}$ 

Momentum [Qian 1999]  $w^{(t+1)} = w^{(t)} + \mu \cdot (w^{(t)} - w^{(t-1)}) - \eta \cdot \nabla w^{(t)}$ 

Nesterov Momentum [Nesterov 1983]  $w^{(t+1)} = w^{(t)} + v_t; \qquad v_{t+1} = \mu \cdot v_t - \eta \cdot \nabla \ell(w^{(t)} - \mu \cdot v_t, z)$ 

AdaGrad [Duchi et al. 2011]  $w_i^{(t+1)} = w_i^{(t)} - \frac{\eta \cdot \nabla w_i^{(t)}}{\sqrt{A_{i,t} + \varepsilon}}; \qquad A_{i,t} = \sum_{\tau=0}^t \left( \nabla w_i^{(t)} \right)^2$ 

RMSProp [Hinton 2012]  $w_{i}^{(t+1)} = w_{i}^{(t)} - \frac{\eta \cdot \nabla w_{i}^{(t)}}{\sqrt{A'_{i,t}} + \varepsilon}; \qquad A'_{i,t} = \beta \cdot A'_{t-1} + (1 - \beta) \left( \nabla w_{i}^{(t)} \right)^{2}$ 

Adam [Kingma and Ba 2015]  $w_i^{(t+1)} = w_i^{(t)} - \frac{\eta \cdot M_{i,t}^{(1)}}{\sqrt{M_{i,t}^{(2)} + \varepsilon}}; \qquad M_{i,t}^{(m)} = \frac{\beta_m \cdot M_{i,t-1}^{(m)} + (1-\beta_m) \left(\nabla w_i^{(t)}\right)^m}{1-\beta_m^t}$ 

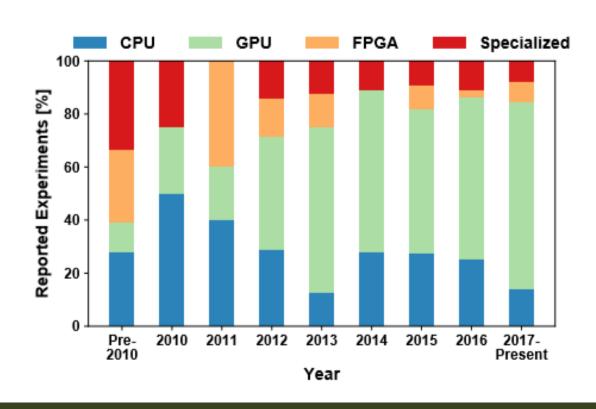


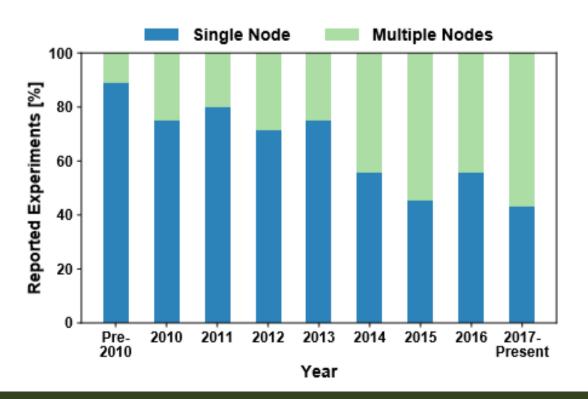




## Trends in deep learning: hardware and multi-node

The field is moving fast – trying everything imaginable – survey results from 227 papers in the area of parallel deep learning





# Deep Learning is largely on distributed memory today!

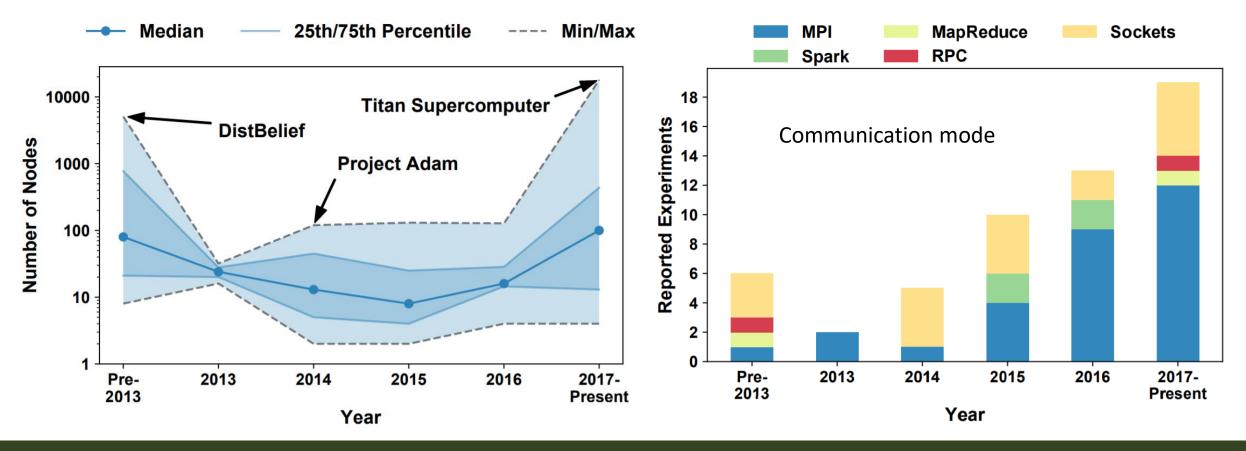






## Trends in distributed deep learning: node count and communication

The field is moving fast – trying everything imaginable – survey results from 227 papers in the area of parallel deep learning



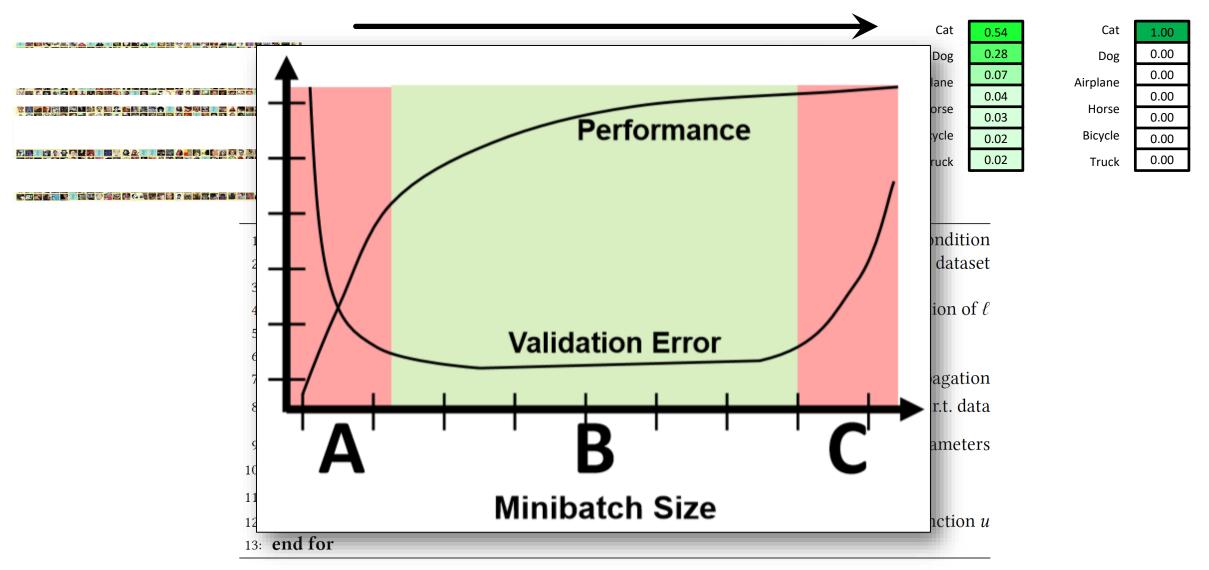
# Deep Learning research is converging to MPI!







## Minibatch Stochastic Gradient Descent (SGD)

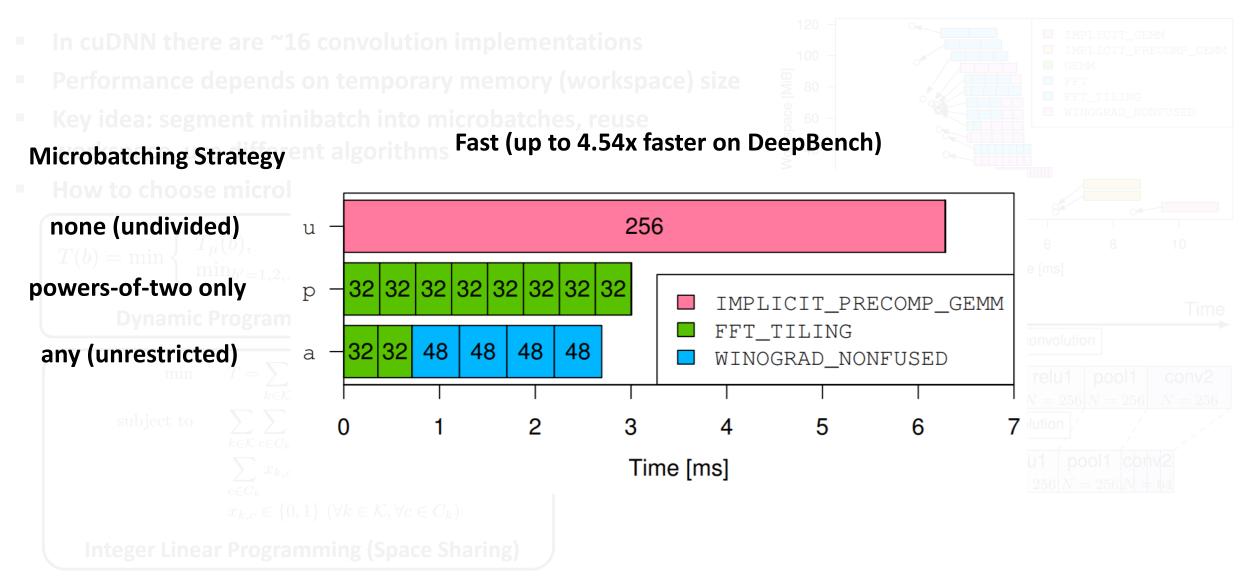








## Microbatching (μ-cuDNN) – how to implement layers best in practice?

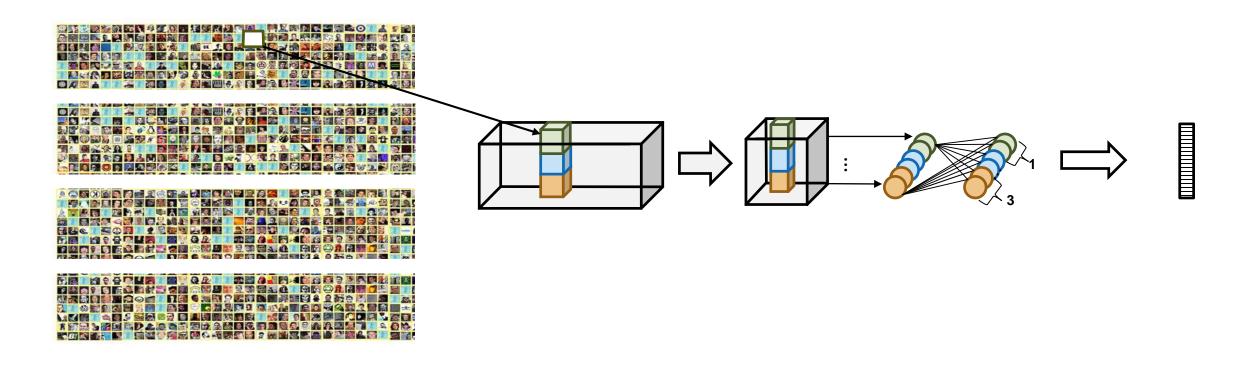








## Model parallelism – limited by network size



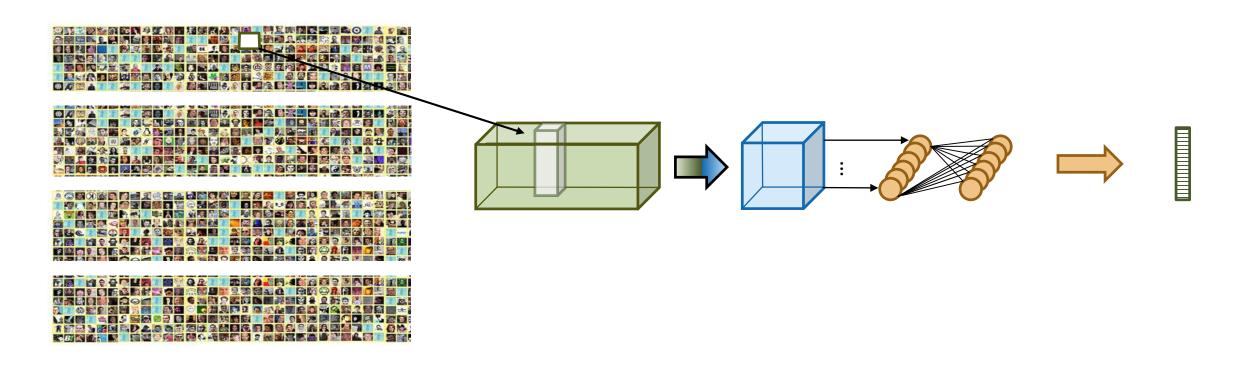
- Parameters can be distributed across processors
- Mini-batch has to be copied to all processors
- Backpropagation requires all-to-all communication every layer







## Pipeline parallelism – limited by network size



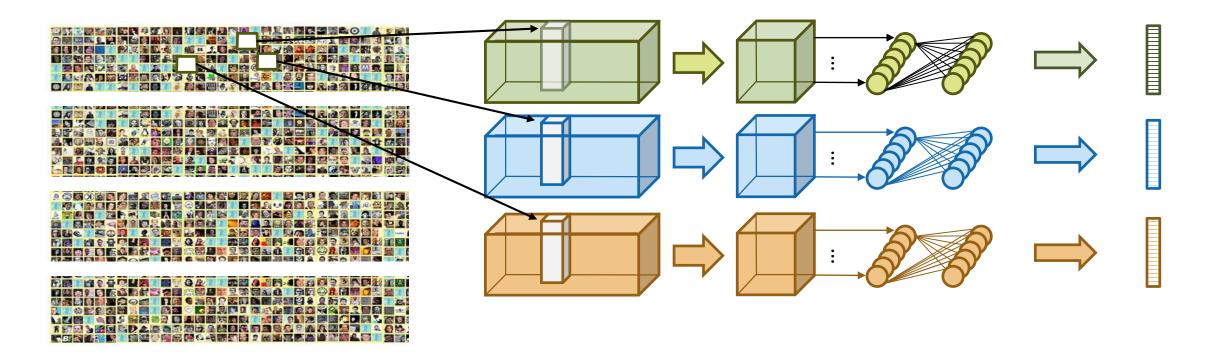
- Layers/parameters can be distributed across processors
- Sparse communication pattern (only pipeline stages)
- Mini-batch has to be copied through all processors







## Data parallelism – limited by batch-size

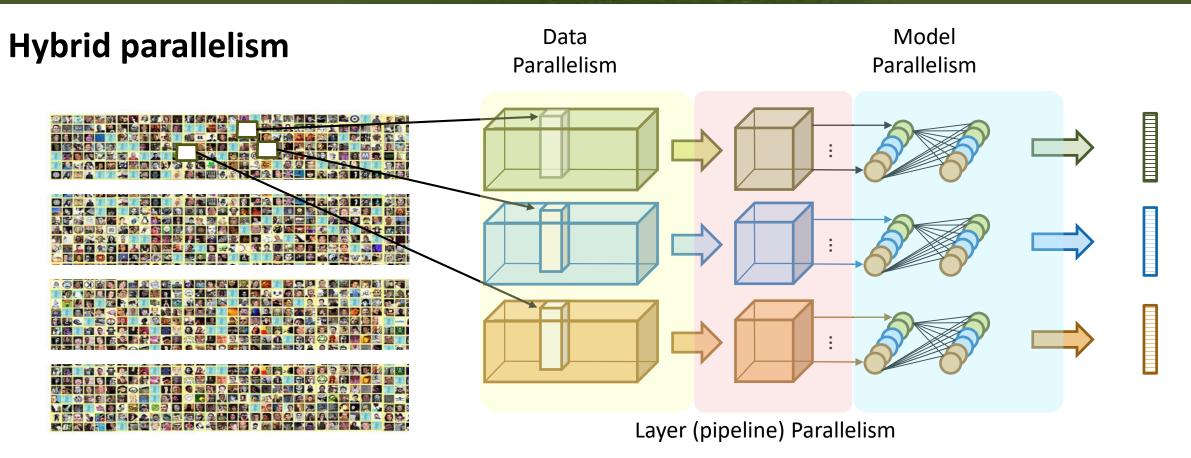


- Simple and efficient solution, easy to implement
- Duplicate parameters at all processors









- Layers/parameters can be distributed across processors
- Can distribute minibatch
- Often specific to layer-types (e.g., distribute fc layers but handle conv layers data-parallel)
  - Enables arbitrary combinations of data, model, and pipeline parallelism very powerful!

A. Krizhevsky: One weird trick for parallelizing convolutional neural networks, arXiv 2014

J. Dean et al.: Large scale distributed deep networks, NIPS'12.

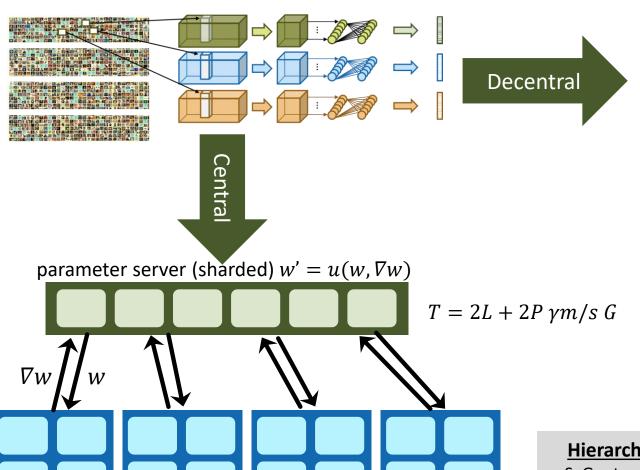
T. Ben-Nun, T. Hoefler: Demystifying Parallel and Distributed Deep Learning: An In-Depth Concurrency Analysis, arXiv Feb 2018

Training Agent Training Agent





## Updating parameters in distributed data parallelism



**Training Agent** 

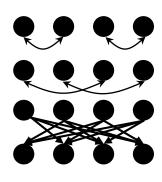
**Training Agent** 







- Topologies
- Neighborhood collectives
- RMA?



 $T = 2L \log_2 P + 2\gamma mG(P-1)/P$ 

#### **Hierarchical Parameter Server**

S. Gupta et al.: Model Accuracy and Runtime Tradeoff in Distributed Deep Learning: A Systematic Study. ICDM'16

#### **Adaptive Minibatch Size**

S. L. Smith et al.: Don't Decay the Learning Rate, Increase the Batch Size, arXiv 2017

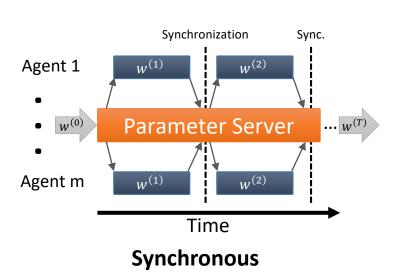


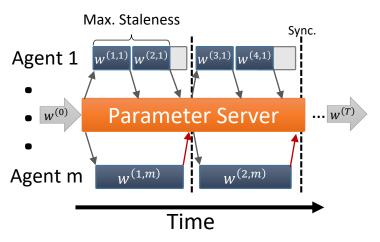




## Parameter (and Model) consistency - centralized

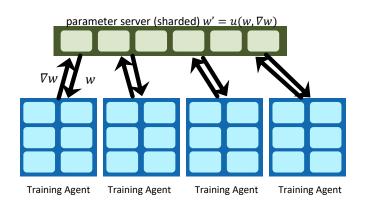
Parameter exchange frequency can be controlled, while still attaining convergence:

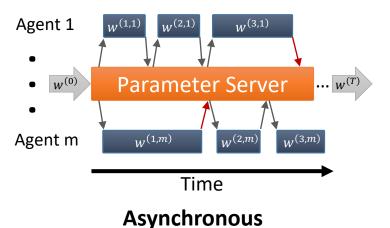




**Stale Synchronous / Bounded Asynchronous** 

- Started with Hogwild! [Niu et al. 2011] shared memory, by chance
- DistBelief [Dean et al. 2012] moved the idea to distributed
- Trades off "statistical performance" for "hardware performance"





J. Dean et al.: Large scale distributed deep networks, NIPS'12.





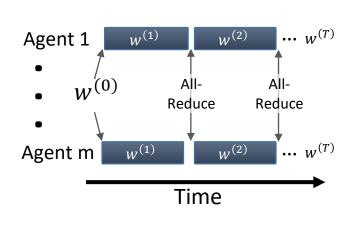


## Parameter (and Model) consistency - decentralized

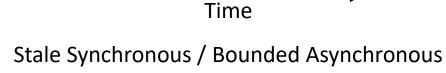
Parameter exchange frequency can be controlled, while still attaining convergence:



Training Agent Training Agent Training Agent Training Agent



Synchronous



Reduce

 $w^{(3,1)} w^{(4,1)}$ 

 $w^{(2,m)}$ 

Merge

Reduce

Max. Staleness

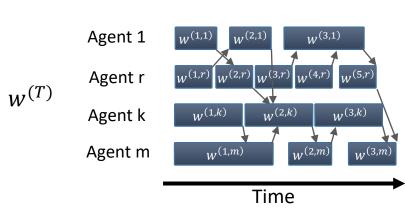
 $_{W_{1}}(1,1)$   $_{W_{2}}(2,1)$ 

 $w^{(1,m)}$ 

Agent 1

Agent m

 $w^{(0)}$ 



Asynchronous

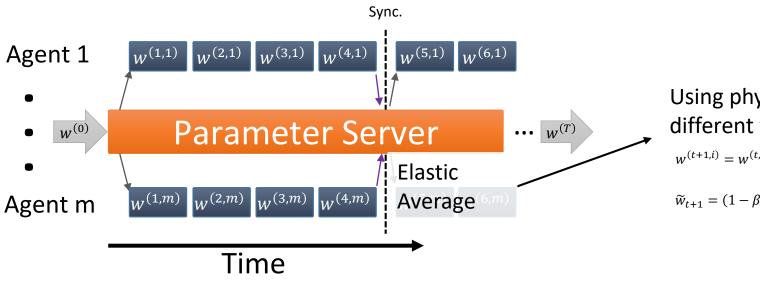
May also consider limited/slower distribution – gossip [Jin et al. 2016]







## Parameter consistency in deep learning



Using physical forces between different versions of w:

$$w^{(t+1,i)} = w^{(t,i)} - \eta \nabla w^{(t,i)} - \alpha (w^{(t,i)} - \widetilde{w}_t)$$

$$\widetilde{w}_{t+1} = (1 - \beta)\widetilde{w}_t + \frac{\beta}{m} \sum_{i=1}^m w^{(t,i)}$$

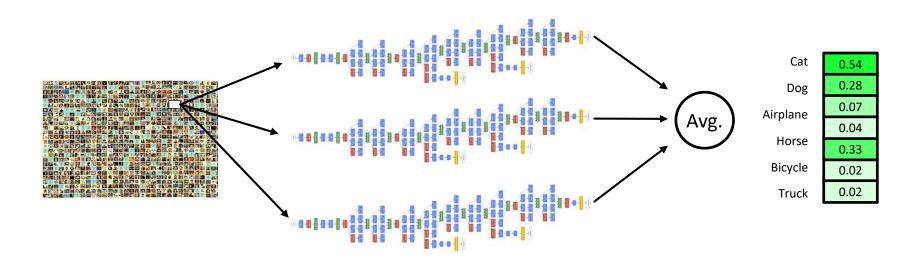


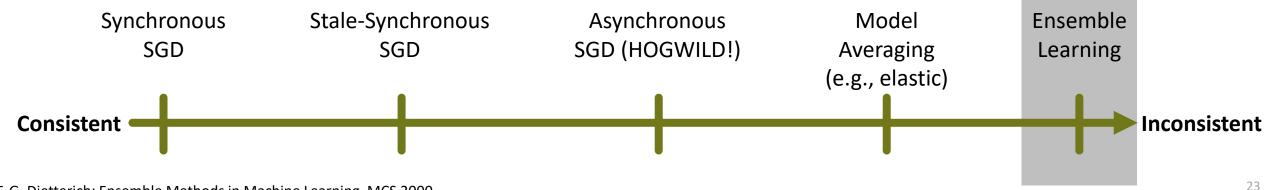






## Parameter consistency in deep learning











## **Communication optimizations**

### Different options how to optimize updates

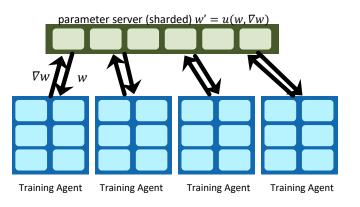
- Send  $\nabla w$ , receive w
- Send FC factors  $(o_{l-1}, o_l)$ , compute  $\nabla w$  on parameter server Broadcast factors to not receive full w
- Use lossy compression when sending, accumulate error locally!

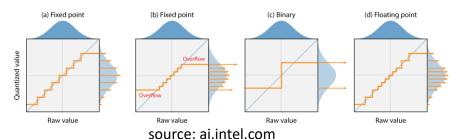
#### Quantization

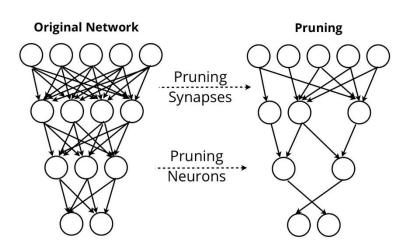
- Quantize weight updates and potentially weights
- Main trick is stochastic rounding [1] expectation is more accurate
   Enables low precision (half, quarter) to become standard
- TernGrad ternary weights [2], 1-bit SGD [3], ...

## Sparsification

Do not send small weight updates or only send top-k [4]
 Accumulate omitted gradients locally







<sup>[1]</sup> S. Gupta et al. Deep Learning with Limited Numerical Precision, ICML'15

<sup>[2]</sup> F. Li and B. Liu. Ternary Weight Networks, arXiv 2016

<sup>[3]</sup> F. Seide et al. 1-Bit Stochastic Gradient Descent and Application to Data-Parallel Distributed Training of Speech DNNs, In Interspeech 2014







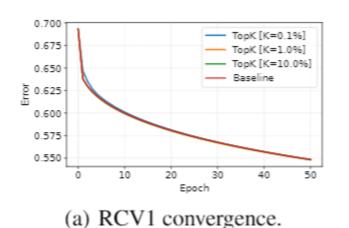
## **Sparsification – top-k Stochastic Gradient Descent**

- Pick the k-largest elements of the vector at each node!
  - Accumulate the remainder locally (convergence proof, similar to async. SGD with implicit staleness bounds [1])

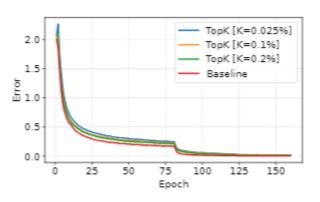
**Assumption 1.** There exists a (small) constant  $\xi$  such that, for every iteration  $t \geq 0$ , we have:

$$\left\| \operatorname{TopK} \left( \frac{1}{P} \sum_{p=1}^{P} \left( \alpha \tilde{G}_t^p(v_t) + \epsilon_t^p \right) \right) - \sum_{p=1}^{P} \frac{1}{P} \operatorname{TopK} \left( \alpha \tilde{G}_t^p(v_t) + \epsilon_t^p \right) \right\| \leq \xi \|\alpha \tilde{G}_t(v_t)\|.$$

**Discussion.** We validate Assumption 1 experimentally on a number of different learning tasks in Section 6 (see also Figure 1). In addition, we emphasize the following points:



200 TopK [K=0.1%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=10.0%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=1.0%]
TopK [K=0.1%]



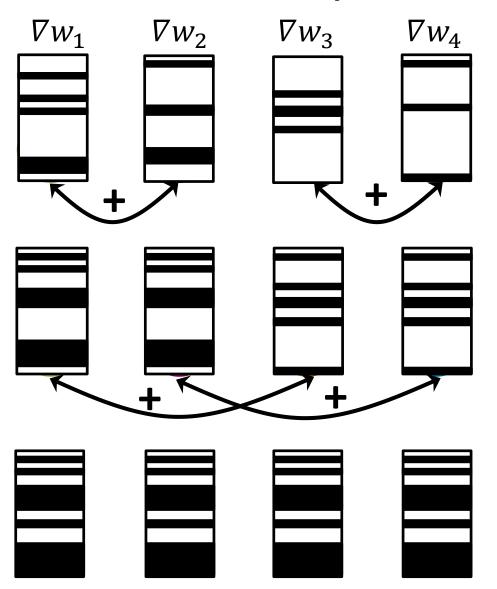
(b) Linear regression.

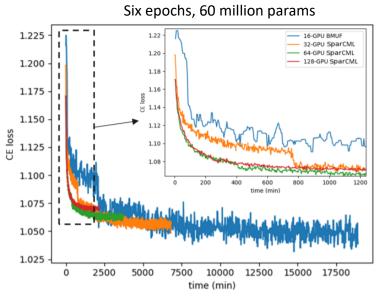
(c) ResNet110 on CIFAR10.

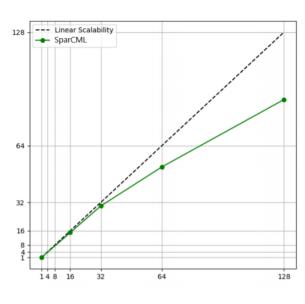




## **SparCML – Quantified sparse allreduce for decentral updates**

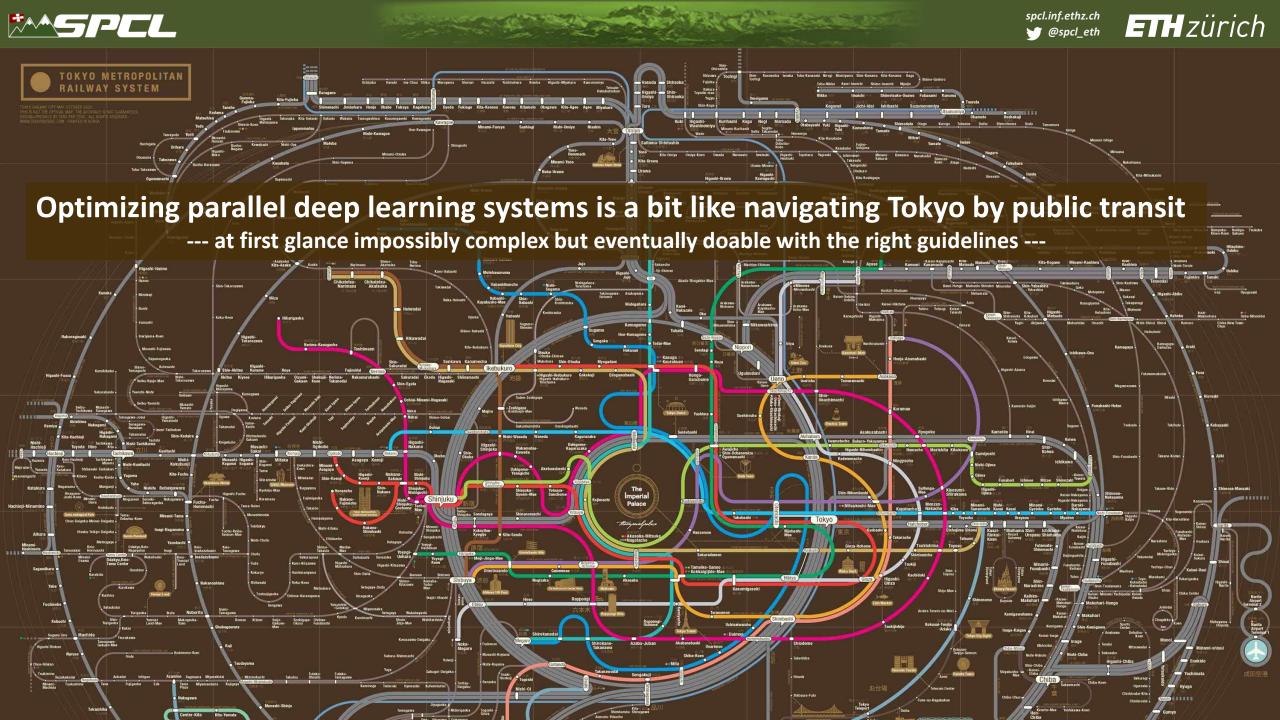






Microsoft Speech Production Workload Results – 2 weeks → 2 days!

System	Dataset	Model	# of nodes	Algorithm	Speedup
Piz Daint	ImageNet	VGG19	8	Q4	1.55 (3.31)
Piz Daint	ImageNet	AlexNet	16	Q4	1.30 (1.36)
Piz Daint   EC2	MNIST	MLP	8	Top16_Q4 Top16_Q4	3.65 (4.53) 19.12 (22.97)



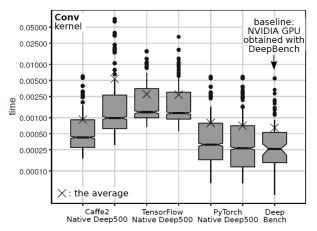


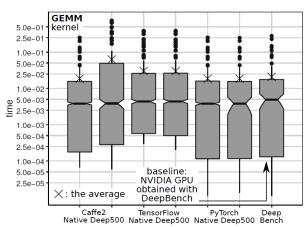


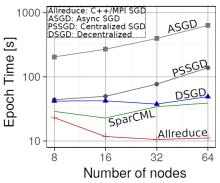


## Deep500: An HPC Deep Learning Benchmark and Competition

- Integrates tensorflow, pytorch, caffee2 into a single benchmarking framework
  - Separate definition of benchmark metrics, shared across all levels
- Lean reference implementations simple to understand and change
  - Operators (layer computations)
  - Optimizers (SGD etc.)
  - Distribution schemes (cf. Horovod) Similar to reference LINPACK benchmark
- **Supports optimization of components** 
  - E.g., no need to reimplement an optimizer to replace gradient compression! Easily compare to all frameworks!







(a) Strong scaling (Wide ResNet 28x10).

Fig. 11: Scaling Analysis of Level 3



500 ways to train DNNs

#### A Modular Benchmarking Infrastructure for High-Performance and Reproducible Deep Learning

Tal Ben-Nun, Simon Huber, Maciej Besta, Alexandros Nikolaos Ziogas, Daniel Peter, Torsten Hoefler Department of Computer Science, ETH Zurich

Abstract.—We introduce Deep500: the first customizable bench. on different platforms, and executing custom algorithms. To ors, network processing, training, and distributed training Our evaluation illustrates that Deep500 is customizable (enables

#### I. INTRODUCTION

Deep Learning (DL) has transformed the world and is now ubiquitous in areas such as speech recognition, image classification, or autonomous driving [3]. Its central concept is a Deep Neural Network (DNN), a structure modeled after the human brain. Thanks to rigorous training, DNNs are able to solve various problems, previously deemed unsolvable.

Recent years saw an unprecedented growth in the number of approaches, schemes, algorithms, applications, platforms, and frameworks for DL. First, DL computations can aim at inference or training. Second, hardware platforms can vary significantly, including CPUs, GPUs, or FPGAs, Third, operators can be computed using different methods, e.g., im2col [5] have been deployed in a variety of frameworks, such as TensorFlow [14] or Caffe [20]. These functionalities may incorporate many parallel and distributed optimizations, such as data, model, and pipeline parallelism. Finally, DL workloads phones, multi-GPU clusters, or large-scale supercomputers.

This richness of the DL domain raises a question we have not seen addressed so far. How can one ensure a leveled, fair ground for comparison, competition, and the recent benchmarking approaches such as DAWNBench [9] or MLPerf [30] are merely lists of results that do not directly consider the rich nature of today's DL efforts.

To answer this question, we propose Deep500: a bench marking system that enables fair analysis and comparison of diverse DL efforts. Deep500 is based on the following five pillars: 

Customizability. 

Metrics. 

Performance. Validation, and 6 Reproducibility. 0 "Customizability" indicates that Deep500 enables benchmarking of arbitrary combinations of DL elements, such as various frameworks running

achieve this, we design Deep500 to be a meta-framework that faster DL programming. @ "Metrics" indicates that Deep500 embraces a complex nature of DL that, unlike benchmarks insufficient measure. To this end, we propose metrics that con sider the accuracy-related aspects of DL (e.g., time required to ensure a specific test-set accuracy) and performance-related ssues (e.g., communication volume), @ "Performance" means can be integrated with parallel and distributed DL codes. 9 "Validation" indicates that Deep500 provides infrastructure to ensure correctness of aspects such as convergence. Finally, HPC initiatives [18] to help developing reproducible DL codes

Table II compares Deep500 to other benchmarking infras tructures with respect to the offered functionalities. Deep500 is the only system that focuses on performance, accuracy, and onvergence, while simultaneously offering a wide spectrum of metrics and criteria for benchmarking, enabling customiz ability of design, and considering a diversity of workloads.









## **HPC for Deep Learning – Summary**

- Deep learning is HPC very similar computational structure, in fact very friendly
  - Amenable to specialization, static scheduling, all established tricks microbatching
- Main bottleneck is communication reduction by trading off

#### **Parameter Consistency**

- Bounded synchronous SGD
- Central vs. distributed parameter server
- EASGD to ensemble learning

#### **Parameter Accuracy**

- Lossless compression of gradient updates
- Quantization of gradient updates
- Sparsification of gradient updates
- Very different environment from traditional HPC
  - Trade-off accuracy for performance!
- Performance-centric view in HPC can be harmful for accuracy!
  - T. Hoefler: "Twelve ways to fool the masses when reporting performance of deep learning workloads" (my humorous guide to floptimization in deep learning will be published this week during IPAM)







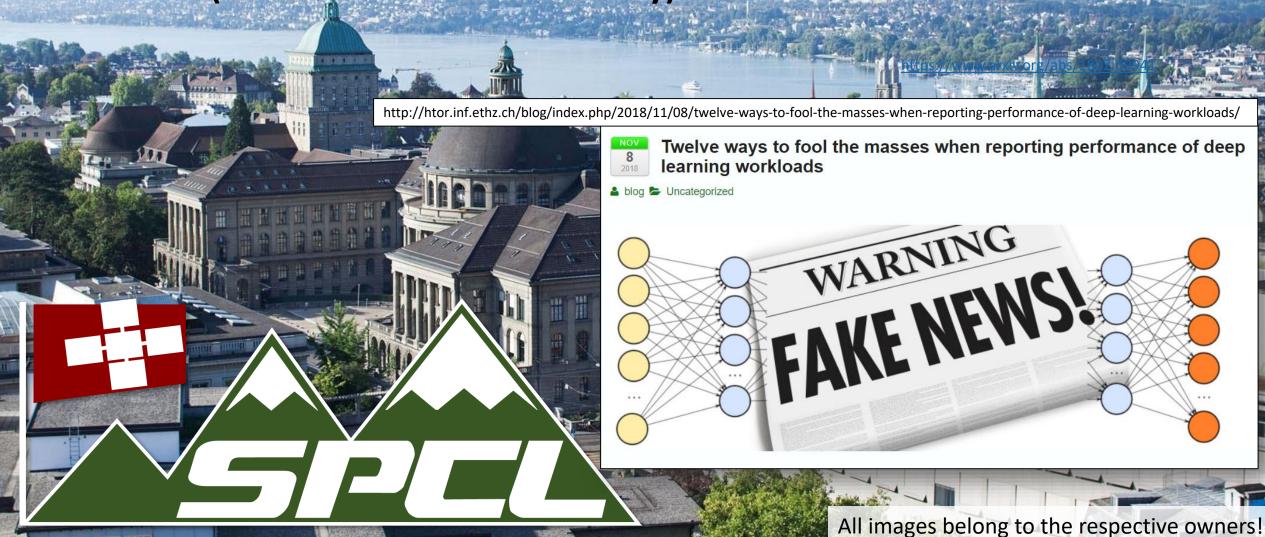
## How to **not** do this

"Twelve ways to fool the masses when reporting performance of deep learning workloads" (my humorous guide to floptimize deep learning, blog post Nov. 2018)



#### T. HOEFLER

Twelve ways to fool the masses when reporting performance of deep learning workloads! (not to be taken too seriously)









## **Deep learning and HPC**

#### Deep learning is HPC

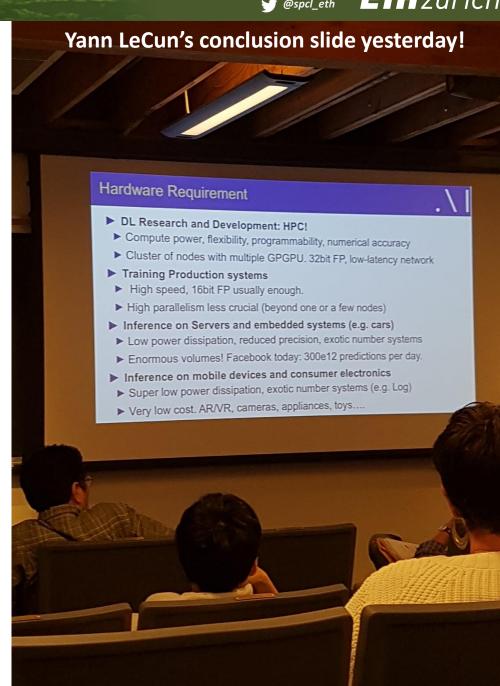
In fact, it's probably (soon?) bigger than traditional HPC
Definitely more money ...

#### Interest in the HPC community is tremendous

Number of learning papers at HPC conferences seems to be growing exponentially Besides at SC18, whut!?

#### Risk of unrealism

- HPC people know how to do HPC
- And deep learning is HPC, right? Not quite ... while it's really similar (tensor contractions) But it's also quite different!









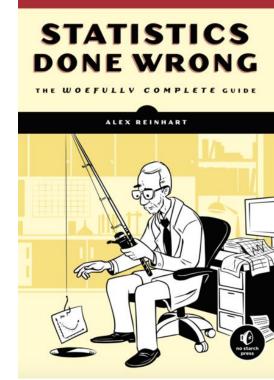
## "Statistical performance" vs. "hardware performance"

- Tradeoffs between those two
  - Very weird for HPC people we always operated in double precision
     Mostly out of fear of rounding issues

- Deep learning shows how little accuracy one can get away with
  - Well, examples are drawn randomly from some distribution we don't know ...
  - Usually, noise is quite high ...
  - So the computation doesn't need to be higher precision than that noise

    Pretty obvious! In fact, it's similar in scientific computing but in tighter bounds and not as well known

- But we HPC folks like flop/s! Or maybe now just ops or even aiops? Whatever, fast compute!
  - A humorous guide to floptimization
  - Twelve rules to help present your (not so great?) results in a much better light



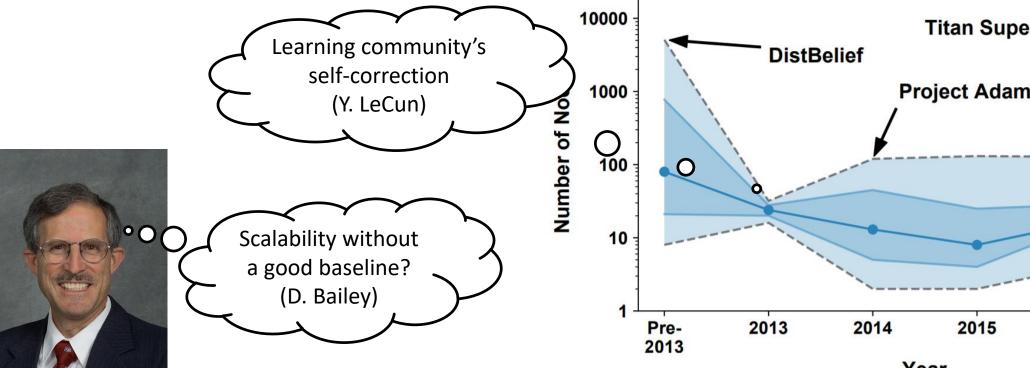




## 1) Ignore accuracy when scaling up!

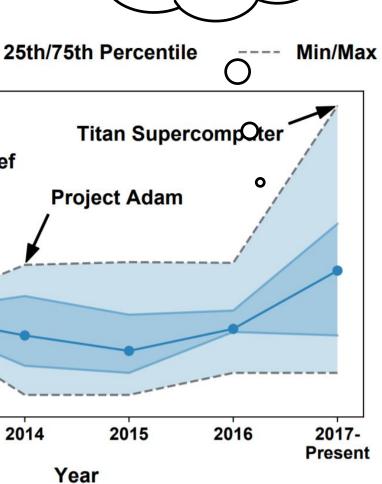
- Too obvious for this audience
  - Was very popular in 2015!





Median





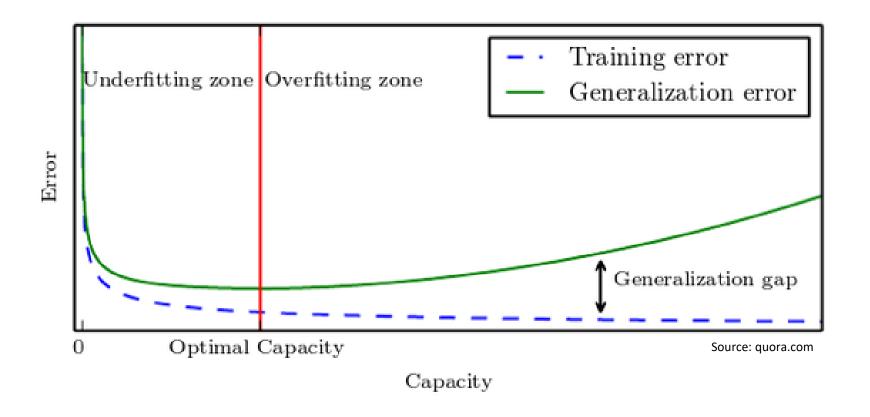






## 2) Do not report test accuracy!

Training accuracy is sufficient isn't it?

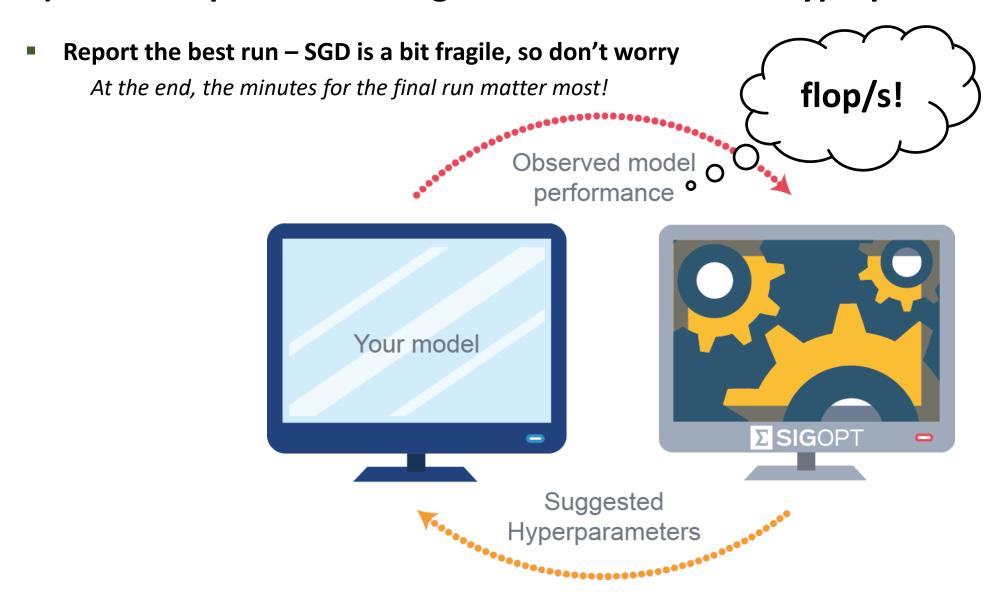








## 3) Do not report all training runs needed to tune hyperparameters!









## 4) Compare outdated hardware with special-purpose hardware!

Tesla K20 in 2018!?

Even though the older machines would win the beauty contest!



VS.









## 5) Show only kernels/subsets when scaling!

- Run layers or communication kernels in isolation
  - Avoids issues with accuracy completely © Doesn't that look a bit like GoogLeNet?



VS.



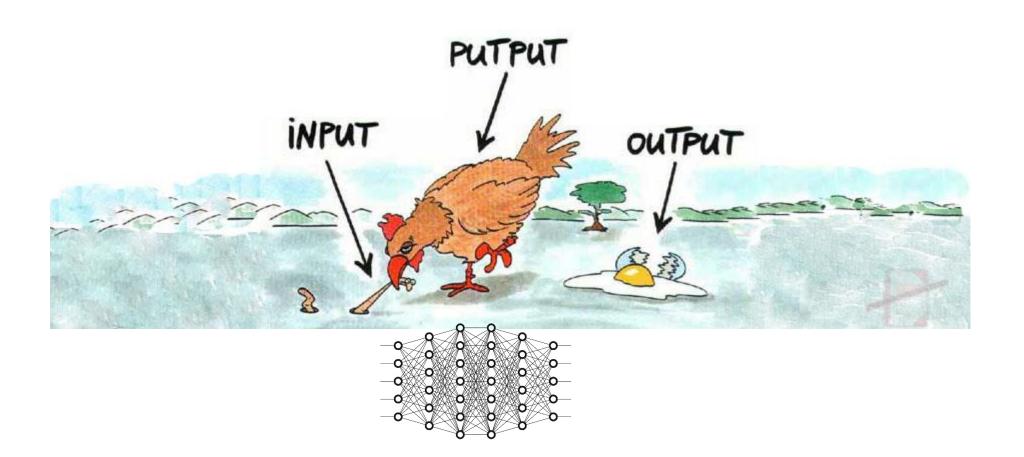






## 6) Do not consider I/O!

Reading the data? Nah, make sure it's staged in memory when the benchmark starts!









## 7) Report highest ops numbers (whatever that means)!

- Yes, we're talking ops today, 64-bit flops was so yesterday!
  - If we don't achieve a target fast enough, let's redefine it!

    And never talk about how many more of those ops one needs to find a solution, it's all about the rate, op/s!
- Actually, my laptop achieves an "exaop":
  - each of the 3e9 transistors switching a binary digit each at 2.4e9 Hz





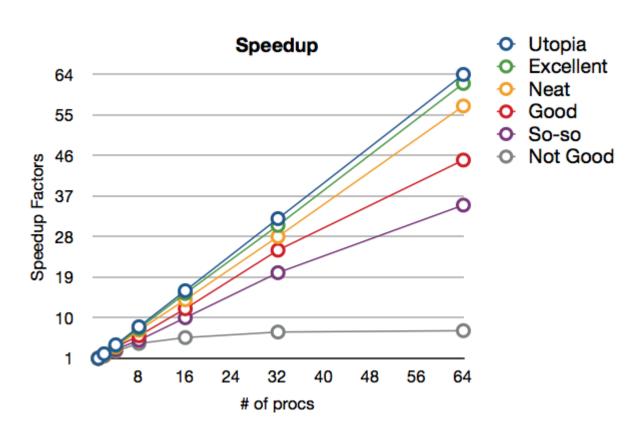


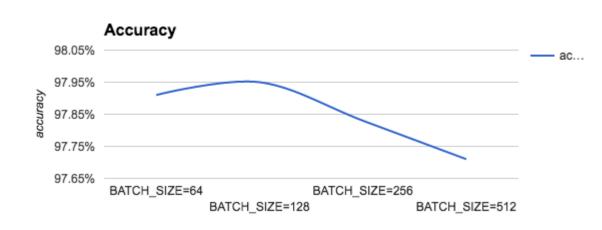


# 8) Show performance when enabling option set A and show accuracy when enabling option set B!

Pretty cool idea isn't it? Hyperparameters sometimes conflict

So always tune the to show the best result, whatever the result shall be!











## 9) Train on (unreasonably) large inputs!

The pinnacle of floptimization! Very hard to catch!

But Dr. Catlock Holmes below can catch it.



VS.

Low-resolution cat (244x244 – 1 Gflop/example)



High-resolution cat (8kx8x – 1 Tflop/example)

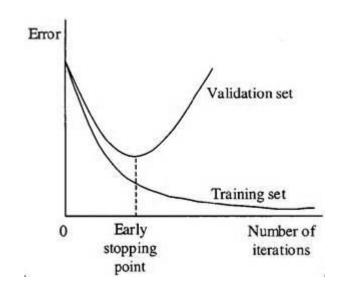




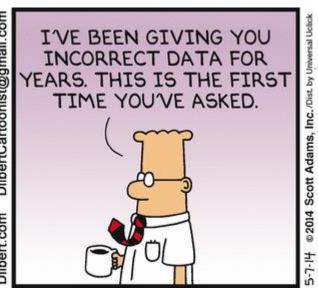


## 10) Run training just for the right time!

- Train for fixed wall-time when scaling processors
  - so when you use twice as many processors you get twice as many flop/s!
    But who cares about application speedup?









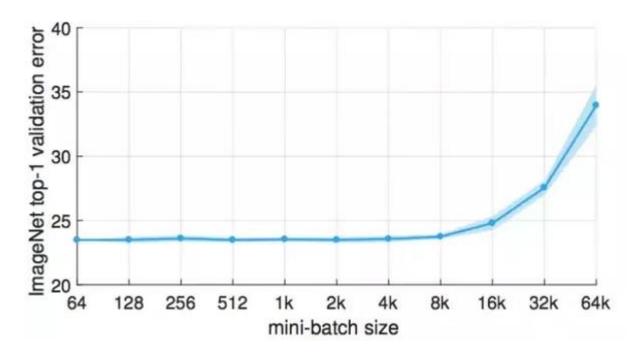






## 11) Minibatch sizing for fun and profit – weak vs. strong scaling.

- All DL is strong scaling limited model and limited data
- So just redefine the terms relative to minibatches:
  - Weak scaling keeps MB size per process constant overall grows (less iterations per epoch, duh!)
  - Strong scaling keeps overall MB size constant (better but harder)
- Microbatching is not a problem!







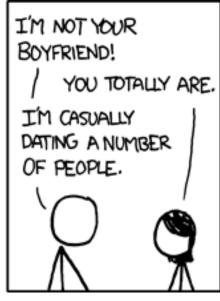


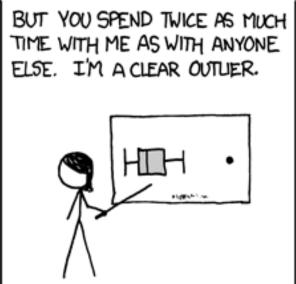
## 12) Select carefully how to compare to the state of the art!

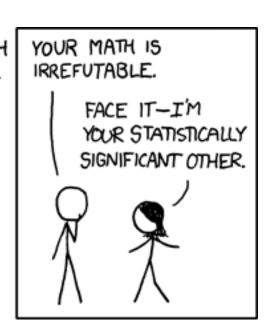
Compare either time to solution or accuracy if both together don't look strong!

There used to be conventions but let's redefine them.









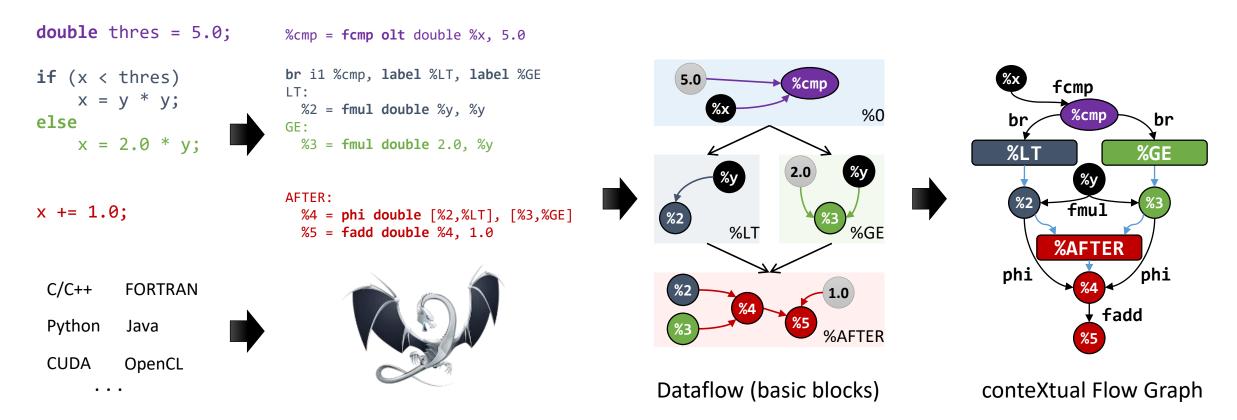






## **Turning 180-degree – Deep Learning for HPC – Neural Code Comprehension**

- In 2017, GitHub reports 1 billion git commits in 337 languages!
- Can DNNs understand code?
- Previous approaches read the code directly  $\rightarrow$  suboptimal (loops, functions)



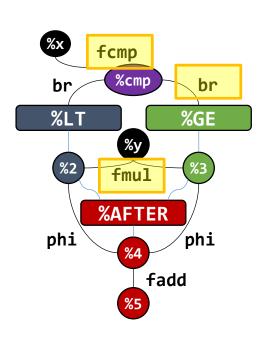


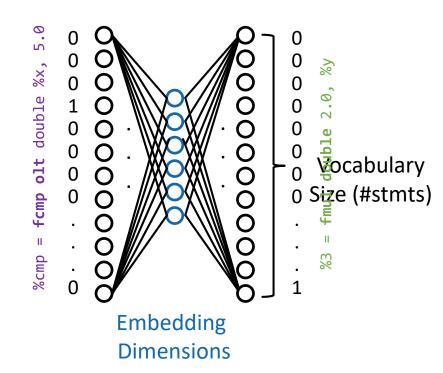




## **Deep Learning for HPC – Neural Code Comprehension**

Embedding space (using the Skip-gram model)











## **Deep Learning for HPC – Neural Code Comprehension**

Embedding space (us

Table 3: Algorithm classification test accuracy

	8		<u> </u>	
Metric	Surface Features 46 (RBF SVM + Bag-of-Trees)	RNN [46]	TBCNN 46	inst2vec
Test Accuracy [%]	88.2	84.8	94.0	94.83

## Predicts which device is faster (CPU or GPU)

Table 4: Heterogeneous device mapping results

Architecture	Prediction Accuracy [%]		Speedup			
	Grewe et al. [27]	DeepTune [17]	inst2vec	Grewe et al.	DeepTune	inst2vec
AMD Tahiti 7970 NVIDIA GTX 970	73.38 72.94	<b>83.68</b> 80.29	82.79 <b>81.76</b>	2.91 1.26	3.34 <b>1.41</b>	<b>3.42</b> 1.39

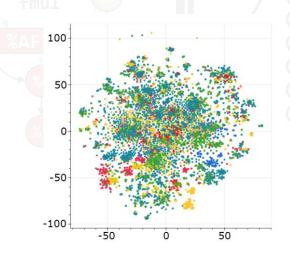
# Optimal tiling US Code Detection

Table 5: Speedups achieved by coarsening threads

Computing Platform	Magni et al. [43]	DeepTune [17]	DeepTune-TL [17]	inst2vec
AMD Radeon HD 5900	1.21	1.10	1.17	1.25
AMD Tahiti 7970	1.01	1.05	1.23	1.07
NVIDIA GTX 480	0.86	1.10	1.14	1.02
NVIDIA Tesla K20c	0.94	0.99	0.93	1.03

Table 2: Analogy and test scores for inst2vec

Context	Syntactic Analogies		Semantic Analogies		Semantic Distance Test
Size	Types	Options	Conversions	Data Structures	
1	101 (18.04%)	13 (24.53%)	100 (6.63%)	3 (37.50%)	60.98%
2	226 (40.36%)	45 (84.91%)	134 (8.89%)	7 (87.50%)	79.12%
3	125 (22.32%)	24 (45.28%)	48 (3.18%)	7 (87.50%)	62.56%



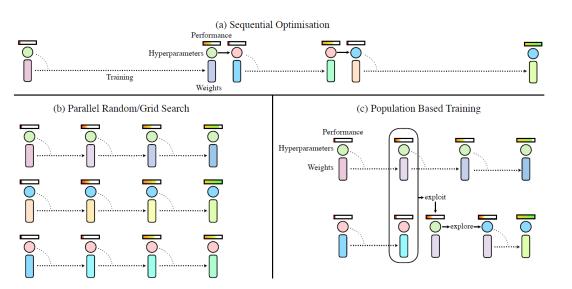


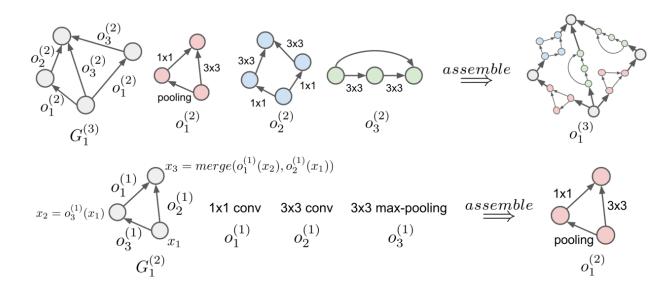




## Hyperparameter and Architecture search

- Meta-optimization of hyper-parameters (momentum) and DNN architecture
  - Using Reinforcement Learning [1] (explore/exploit different configurations)
  - Genetic Algorithms with modified (specialized) mutations [2]
  - Particle Swarm Optimization [3] and other meta-heuristics

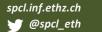




## **Reinforcement Learning [1]**

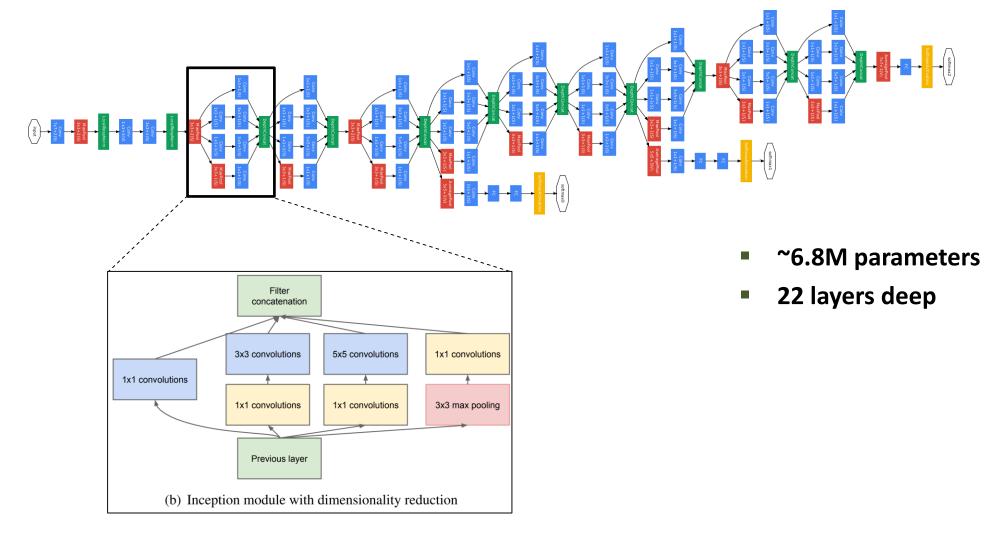
### **Evolutionary Algorithms [4]**

- [1] M. Jaderberg et al.: Population Based Training of Neural Networks, arXiv 2017
- [2] E. Real et al.: Regularized Evolution for Image Classifier Architecture Search, arXiv 2018
- [3] P. R. Lorenzo et al.: Hyper-parameter Selection in Deep Neural Networks Using Parallel Particle Swarm Optimization, GECCO'17
- [4] H. Liu et al.: Hierarchical Representations for Efficient Architecture Search, ICLR'18





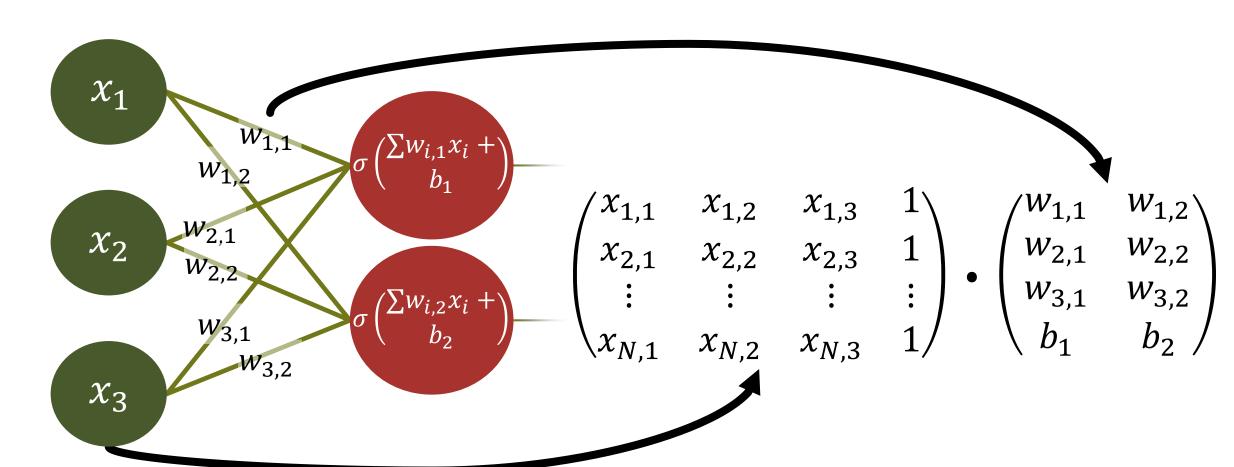
## **GoogLeNet** in more detail





## **Computing fully connected layers**

$$\begin{array}{lll} f_l(x) & O(C_{out} \cdot C_{in} \cdot N) & O(\log C_{in}) \\ \nabla w & O(C_{in} \cdot N \cdot C_{out}) & O(\log N) \\ \nabla o_l & O(C_{in} \cdot C_{out} \cdot N) & O(\log C_{out}) \end{array}$$









## **Computing convolutional layers**

	b a a9 a .				
	Direct		Indirect		
	4 1 9 8	1 -1 0 21.9 59.3 53.9 43.9	FFT	Winograd	
Dire	Method	Work (W)	Depth (D)		
	Direct	$N \cdot C_{out} \cdot H' \cdot W' \cdot C_{in} \cdot K_y \cdot K_x$	$\lceil \log_2 C_{in} \rceil + \lceil \log$	$g_2 K_y + \lceil \log_2 K_x \rceil$	
	im2col	$N \cdot C_{out} \cdot H' \cdot W' \cdot C_{in} \cdot K_y \cdot K_x$	$\lceil \log_2 C_{in} \rceil + \lceil \log$	$g_2 K_y + \lceil \log_2 K_x \rceil$	
	FFT	$c \cdot HW \log_2(HW) \cdot (C_{out} \cdot C_{in} + N \cdot C_{in} + N \cdot C_{out}) + HWN \cdot C_{in} \cdot C_{out}$	$2 \lceil \log_2 HW \rceil + \lceil \log_2 C_{in} \rceil$ $2 \lceil \log_2 r \rceil + 4 \lceil \log_2 \alpha \rceil + \lceil \log_2 C_{in} \rceil$		
im2	Winograd $(m \times m \text{ tiles},$	$\alpha(r^2 + \alpha r + 2\alpha^2 + \alpha m + m^2) + C_{out} \cdot C_{in} \cdot P$			
	$r \times r$ kernels)	$(\alpha \equiv m - r + 1,  P \equiv N \cdot \lceil H/m \rceil \cdot \lceil W/m \rceil)$			
•	G0 G1 G2 G3 G0	G1 G2 G3 G0 G1 G2 G3		Activation Layer i + 1	

K. Chellapilla et al.: High Performance Convolutional Neural Networks for Document Processing, Int'l Workshop on Frontiers in Handwriting Recognition 2016 M. Mathieu et al.: Fast Training of Convolutional Networks through FFTs, ICLR'14